# **AP Calculus AB**

<u>Teachers</u>

Michael Hernández

MIT 2014

mhernand@mit.edu

Esteban Madrigal

Harvard 2014

madrigal@college.harvard.edu

## Prerequisites

Those outlined by the College Board at http://www.collegeboard.com/student/testing/ap/sub\_calab.html?calcab

"Before studying calculus, all students should complete four years of secondary mathematics designed for college-bound students: courses in which they study algebra, geometry, trigonometry, analytic geometry, and elementary functions. These functions include those that are linear, polynomial, rational, exponential, logarithmic, trigonometric, inverse trigonometric, and piecewise defined. In particular, before studying calculus, students must be familiar with the properties of functions, the algebra of functions, and the graphs of functions. Students must also understand the language of functions (domain and range, odd and even, periodic, symmetry, zeros, intercepts, and so on) and know the values of the trigonometric functions of the numbers 0, pi/6, pi/4, pi/3, pi/2, and their multiples."

## <u>Homework</u>

Problem sets and their solutions will be provided, but will not be collected. It is expected that you complete the problem set and then check your solutions. If anything is still unclear after the solutions have been posted then you should ask us for help.

### <u>Quizzes</u>

Every class will have 1-2 very short quizzes; they will last no longer than 15 minutes each. We will use these to assess the class' understanding of the material and to make any changes to the pace of the lessons. The quizzes will be more conceptual than computational, i.e. they might require more writing than calculator work. Therefore, it is essential to have an intuitive understanding of calculus. Memorizing methods for solving problems will not be enough.

## Structure of Class time

Classes will consist of lecture, class work, and quizzes. We will have a 10 minute break for every 2 hour block.

#### Lessons

#### Class

#### s Lesson 1 Part 1: The Limit Process

An Introduction to the Limit Process

Finding Limits Graphically and Numerically

2 Finding Limits Analytically Continuity and One-sided Limits Infinite Limits/Vertical Asymptotes

#### 3 Part 2: Derivatives

The Tangent Line Problem

- 4 Basic Differentiation Rules Rates of Change The Product and Quotient rules
- 5 Derivatives of Trigonometric Functions Higher Order Derivatives
- 6 The Chain Rule Implicit Differentiation
- 7 Related Rates
- 8 Continuation of Lesson 7
- 9 Extrema on an Interval

Rolle's Theorem and the Mean Value Theorem

Increasing and Decreasing Functions and the First Derivative Test

Concavity and the Second Derivative Test

- 10 Limits at infinity/Horizontal Asymptotes Curve Sketching
- 11 Continuation of Lesson 10

- 12 Optimization Problems
- 13 Continuation of Lesson 12
- 14 Newton's Method Differentials
- 15 Part 3: Integration

Antiderivatives

- 16 The Fundamental Theorems of Calculus
- 17 Integration by Substitution
- 18 The Natural Logarithm Function Exponentials
- 19 Integrations Tables
- 20 Areas between Curves
- 21 Disc Method Shell Method Volumes of Cross Sections
- 22 Continuation of Lesson 20
- 23 Differential Equations Slope Fields
- 24 Integration by Parts
- 25 Continuation of Lesson 23
- 26 Review/Mock AP Test
- 27 Review/Mock AP Test
- 28 Review/Mock AP Test
- 29 Review/Mock AP Test

Review/Mock AP Test